

# GLOBAL JOURNAL OF ENGINEERING SCIENCE AND RESEARCHES THE EDGE FIXING EDGE-TO-VERTEX DETOUR NUMBER OF A GRAPH N.Arianayagam<sup>\*1</sup> and J.John<sup>2</sup>

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# ABSTRACT

We introduce the concept of the total edge fixing edge-to-vertex detour set of a connected graph G. Let e be an edge of a graph G. A set  $S(e) \subseteq E(G) - \{e\}$  is called an edge fixing edge-to-vertex detour set of a connected graph G if every edge of G lies on an e - f detour, where  $f \in S(e)$ . The edge fixing edge-to-vertex detour number defev(G) of G is the minimum cardinality of its edge fixing edge-to-vertex detour sets and any edge fixing edge-to-vertex detour set of cardinality  $dn_{efev}(G)$  is an  $d_{efev}$ -set of G. Connected graphs of order p with edge fixing edge-to-vertex detour number 1 or q - 1 are characterized. The edge fixing edge-to-vertex detour number for some standard graphs are determined. It is shown that for every pair of positive integers with  $2 \le a \le b$ , there exists a connected graph G such that  $dn_{efv}(G) = a$  and  $dn_{efev}(G) = b$ , for some edge  $e \in E(G)$ .

**Keywords:** detour set ,edge-to-vertex detour set , edge fixing edge –to-vertex detour set,edge fixing edge - to vertex detour number. *Mathematical subject classification 05C12.* 

# I. INTRODUCTION

For a graph G = (V, E), we mean a finite undirected graph without loops or multiple edges. The order and size of G are denoted by p and q respectively. We consider connected graphs with at least two vertices. For basic definitions and terminologies we refer to [1,4]. For vertices u and v in a connected graph G, the *detour distanceD*(u, v) is the length of the longest u - v path in G. A u - v path of length D(u, v) is called a u - vdetour. It is known that the detour distance is a metric on the vertex set V(G). The *detour eccentricitye*<sub>D</sub>(v) of a vertex v in G is the maximum detour distance form v to a vertex of G. The detour *radius*,  $rad_D Gof G$  is the minimum detour eccentricity among the vertices of G, while the *detour diameter*,  $diam_D Gof G$  is the maximum detour eccentricity among the vertices of G. These concept were studied by Chartrand et al.[2]. Let G = (V, E) be a connected graph with at least 3 vertices. A set  $S \subseteq E$  is called an *edge-to-vertex detour set* if every vertex of G is either incident with an edge of S or lies on a detour joining a pair of edges of S. The *edge-to-vertex detour numberd*<sub>ev</sub>(G) of G is an *edge-to-vertex detourd*<sub>ev</sub>-set of G.

#### Theorem 1.1[6]

Every pendant edge of a connected graph G belongs to every edge-to-vertex detour set of G.

#### **Theorem 1.2[6]**

For any non-trivial tree T with pendant edges,  $d_{ev}(T) = k$  and the set of all pendant edges of T is the unique minimum edge-to- vertex detour set of T.

#### II. THE EDGE FIXING EDGE-TO-VERTEX DETOUR

# Number of a Graph

# Definition 2.1

Let e be an edge of a graph G. A set  $S(e) \subseteq E(G) - \{e\}$  is called an *edge fixing edge-to-vertex detour set* of a connected graph G if every edge of G lies on an e - f detour, where  $f \in S(e)$ . The *edge fixing edge-to-vertex* 

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detour number  $d_{efev}(G)$  of G is the minimum cardinality of its edge fixing edge-to-vertex detour sets and any edge fixing edge-to-vertex detour set of cardinality  $d_{efev}(G)$  is an  $d_{efev}$ -set of G.

#### Example 2.2

For the graph G given in Figure 2.1, the edge fixing edge-to-vertex detour sets of each edge of G is given in the following Table 2.1.

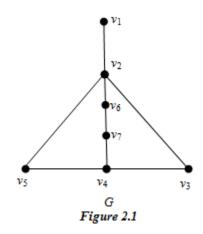


Table	21
1 uvie	4.1

Fixing Edge	Minimum edge fixing edge-to-vertex	$d_{efev}(S(e))$
(e)	detour sets (S(e))	
<i>v</i> <sub>1</sub> <i>v</i> <sub>2</sub>	$\{v_2v_6\},\{v_6v_7\}$	1
<i>v</i> <sub>2</sub> <i>v</i> <sub>3</sub>	$\{v_1v_2,v_6v_7\}$	2
<i>v</i> <sub>3</sub> <i>v</i> <sub>4</sub>	$\{v_1v_2, v_4v_5\}$	2
<i>V</i> <sub>4</sub> <i>V</i> <sub>5</sub>	$\{v_1v_2, v_3v_4\}$	2
$v_2 v_5$	$\{v_1v_2, v_6v_7\}$	2
v <sub>6</sub> v <sub>2</sub>	$\{v_1v_2\}$	1

#### Remark 2.3

For a connected graph *G*, the edge *e* of *G* does not belong to the edge fixing edge-to- vertex detour set *S*(*e*). Also the edge fixing edge-to- vertex detour set of an edge *e* is not unique. For the graph *G* given in Figure 6.1, the edge fixing edge-to- vertex detour sets of the edge  $v_1v_2$  are  $\{v_6v_7\}, \{v_2v_6\}$ .

# III. SOME RESULTS ON THE EDGE FIXING EDGE-TO-VERTEXDETOURNUMBER OF A GRAPH

#### Theorem 2.4

Let *e* be an edge of *G*. Let *f* be a pendant edge of a connected graph *G* such that  $e \neq f$ . Then every edge fixing edgeto- vertex detour set of *e* of *G* contains *f*.

**Proof.** Since  $e \neq f, f$  is a terminal edge of a detourhence *f* belongs to every edge fixing edge-to- vertex detour set of *e*of*G*.

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#### [Arianayagam, 5(3): March 2018] DOI- 10.5281/zenodo.1210092 Theorem 2.5

# Let G be a connected graph and S(e) be an edge fixing edge-to- vertex detour set of e of G. Let f be a non-pendant cut edge of G and let $G_1$ and $G_2$ be the two component of $G - \{f\}$ . If e = f, then each of the two component of $G - \{f\}$ contains an element of S(e). If $e \neq f$ , then S(e) contains at least one edge of component of $G - \{f\}$ where e does not lie.

**Proof.** Let f = uv. Let  $G_1$  and  $G_2$  be the two component of  $G - \{f\}$  such that  $u \in V(G_1)$  and  $\in V(G_2)$ . Let e = f. Suppose that S(e) does not contain any element of  $G_1$ . Then  $S(e) \subseteq E(G_2)$ . Let h be an edge of  $E(G_1)$ . Then h must lie on an e - f' detourforsome  $f' \in S(e)$ . But such a detour  $P: v, v_1, v_2, ..., v_l, v, u, u_1, u_2, ..., u_s, u, v, v_1, v_2, ..., v'$  where  $v_1, v_2, ..., v_l \in V(G_2)$ ,  $u_1, u_2, ..., v_s \in V(G_1)$  and v' is an end of f' has the cut-edge f twice, hence it is a contradiction. This proves the theorem. By similar argument, we can prove that if  $e \neq f$ , then S(e) contains at least one edge from a component of  $G - \{f\}$  where e does not lie.

#### Theorem 2.6

Let G be a connected graph and S(e) be a minimum edge fixing edge-to- vertex detour set of an edge e of G. Then no non-pendant cut-edge of G belongs to S(e).

**Proof.**Let S(e) be an edge fixing edge-to- vertex detour set of an edge e = uvof G. Let f = u'v' be a non-pendant cut-edge of G such that  $f \in S(e)$ . Since  $e \neq f$ , let  $G_1$  and  $G_2$  be the two component of  $G - \{f\}$  such that  $u' \in V(G_1)$  and  $v' \in V(G_2)$ . By Theorem 6.5,  $G_1$  contains an edge xy and  $G_2$  contains an edge x'y' where  $xy, x'y' \in S(e)$ . Let  $S'(e) = S(e) - \{f\}$ . We claim that S'(e) is an edge fixing edge-to- vertex detour set of an edge eof G.

**Case 1.** Suppose that e = xy is an edge in  $G_1$  and x'y' is an edge in  $G_2$ . Let *h* be avertex of *G*. Assume without loss of generality that h = wz belongs to  $G_1$ . Since u'v' is a cut-edge of *G*, every path joining an edge of  $G_1$  with an edge of  $G_2$  contains the edge u'v'. Suppose that *h* is adjacent with u'v' or the edge xy of S(e) or that lies on a detour joining xy and u'v'. If *h* is adjacent with u'v', then z = u'. Let  $P : x, y, y_1, y_2, \ldots, w, z = u$  beaxy -u'v' detour. Let  $Q: u', v', v_1', v_2', \ldots, x', y' a u'v' x'y'$  detour. Then, it is clear that *P* followed by u'v' and *Q* is a xy - x'y' detour. Thus *h* lies on the xy - x'y' detour. If *h* is adjacent with xy, then there is nothing to prove. If *h* lies on a xy - x'y' detour, say  $x, y, v_1, v_2, \ldots, w, z, \ldots, u', v'$ , then let  $u', v', v_1', v_2', \ldots, y'$  be u'v' x'y' detour. Thenclearly $x, y, v_1, v_2, \ldots, w, z, \ldots, u', v'$ , then let  $u', v', v_1', v_2', \ldots, y'$  be u'v' x'y' detour. Thenclearly $x, y, v_1, v_2, \ldots, w, z, \ldots, u', v', y'$  is a xy - x'y' detour. Thus *h* lies on a detour joining xy and u'v' of S(e) also is adjacent with an edge of S'(e) or lies on a detour joining e and an edge of S'(e). Hence it follows that S'(e) is an edge fixing edge-to- vertex detour set of an edge e of G such that |S'(e)| = |S(e)| - 1, which is a contradiction to the minimality of S(e).

**Case 2.**Suppose that  $e = xy \in G_2$ . The proof is similar to that of Case 1. Hence the theorem follows.

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#### Theorem 2.7

For any non-trivial tree *T* with *k*end edges,

 $d_{efev}(G) = \begin{cases} k-1 & \text{if } e \text{ is an end edge of } G \\ k & \text{if } e \text{ is an internal edge of } G \end{cases}$ 

**Proof.** This follows from Theorem 2. 4 and Theorem 2. 6.

#### Theorem 2.8

For the graph  $G = C_p(p \ge 4)$ ,  $d_{efev}(G) = 1$ , for any edge e of E(G).



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**Proof.** Let  $C_p: v_1, v_2, v_3, ..., v_p$  be the cycle. Let *e* be an edge of  $C_p$  and *f* be an edge adjacent to *e*. Then it follows that  $\{f\}$  is an edge fixing edge-to- vertex detour set of an edge *e* of  $C_p$ . Hence  $d_{efev}(C_p) = 1$ .

#### Theorem 2.9

For the complete graph  $K_v(p \ge 4)$ ,  $d_{efev}(G) = 1$  for every edge in E(G).

**Proof.** We observe that all the edges of  $K_p$  can be considered as the edges of  $C_p$  and every edge joining the points of  $C_p$ . Let *e*be an edge of  $C_p$  and *f* be an edge adjacent to *e*. Then it follows that  $\{f\}$  is an edge fixing edge-to-vertex detour set of an edge *e* of  $C_p$ . Hence  $d_{efev}(K_p) = 1$ .

#### Theorem 2.10

Let *G* be a connected graph with at least three vertices. Then  $1 \le d_{efev}(G) \le q - 1$ .

**Proof.** For any edge e in G, an edge fixing edge-to-vertex detour set needs at least one edge of G so that  $d_{efev}(G) \ge 1$ . For an edge  $e \in E(G)$ ,  $E(G) - \{e\}$  is an edge fixing edge-to-vertex detour set of e of G so that  $d_{efev}(G) \le q - 1$ . Therefore  $1 \le d_{efev}(G) \le q - 1$ .

#### Remark 2.11

The bounds in Theorem 2.10 are sharp. For the cycle  $G = C_p$   $(p \ge 4)$ , for an edge e, any edge which is adjacent to e is its minimum edge fixing edge-to-vertex detour set of e of G so that  $d_{efev}(G) = 1$ . For the star  $G = K_{1,q}$ , for an edge e, the set of edges  $E(G) - \{e\}$  is the unique edge fixing edge-to-vertex detour set of e of G so that  $d_{efev}(G) = q - 1$ . Thus the star  $K_{1,q}$  has the largest possible edge fixing edge-to-vertex detour number q - 1 and the cycle  $G = C_p$   $(p \ge 4)$ , has the smallest edge fixing edge-to-vertex detour number 1. Also the bounds in Theorem 2.10 is strict. For the graph G given in Figure 2.1, for the edge  $e = v_3v_4$ ,  $d_{efev}(G) = 2$  so that  $1 < d_{efev}(G) < q - 1$ .

#### Theorem 2.12

Let G be a connected graph of size  $q \ge 3$ , such that G is neither a star nor a double star. Then  $d_{efev}(G) \le q - 2$  for every  $e \in E(G)$ .

#### Proof.

**Case 1.** Suppose that G is a tree such that G is neither a star nor a double star. Then by Theorem 2.7,  $d_{efev}(G) \le q-2$ , for every  $e \in E(G)$ .

Case 2. Suppose that G is not a tree. Then G contains at least one cycle, say C. Let e be an edge of G

Subcase 2a.Suppose that  $e \in E(C)$ . Then S(e) = E(G) - E(C) is an edge fixing edge-to-vertex detour set of an edge *e* of *G* so that  $d_{efev}(G) \le q - 2$ .

**Subcase 2b.** Suppose that  $e \notin E(C)$ . Then setting  $S(e) = E(G) - E(C) - \{e\}$  and by the similar argument in Subcase2a we can prove that  $d_{efev}(G) \le q - 2$ . Hence the proof.

#### Remark 2.13

The bound in Theorem 2.12 is sharp. For the graph  $G = C_3$ , it is easily verified that  $d_{efev}(G) = q - 2$  for every edge eof G.

#### Theorem 2.14

Let *G* be a connected graph of size  $q \ge 2$  and  $e \in E(G)$ . Then  $d_{efev}(G) = q - 1$  if and only if *e* is an edge of  $K_{1,q}$  or *e* is an internal edge of a double star.



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**Proof.** Let G be a connected graph. If e is an edge of  $K_{1,q}$ , then by Theorem 2.7,  $d_{efev}(G) = q - 1$ . If e is an internal edge of a double star, then by Theorem 2.7,  $d_{efev}(G) = q - 1$ .

Conversely, let  $d_{efev}(G) = q - 1$  for an edge  $e \in E(G)$ . Suppose that *e* is neither an edge of  $K_{1,q}$  nor an internal edge of a double star. Then by Theorem 2.12,  $d_{efev}(G) = q - 2$ , which is a contradiction. Therefore *e* is an edge of  $K_{1,q}$  or *e* is an internal edge of a double star.

#### Theorem 2.15

Let *G* be a connected graph with  $q \ge 4$ , which is not a cycle and not a tree and let C(G) be the length of the longest cycle. Then  $d_{efev}(G) \le q - C(G) + 1$  for some  $e \in E(G)$ .

**Proof.** Let C(G) denote the length of the longest cycle in G and C be the cycle of length k.

Let  $C: v_1, v_2, v_3, ..., v_k$  be a cycle,  $k \ge 3$ . Since G is not a cycle, there exists a vertex vin G such that v is not a vertex of C and which is adjacent to  $v_1$ , say. Let e be an edge of C. Let  $S(e) = E(G) - \{E(C) - e\}$ . Clearly S(e) is an edge fixing edge-to-vertex detour set of eofG so that  $d_{efev}(G) \le q - C(G) + 1$ .

#### Theorem 2.16

Let G be a connected graph of size  $q \ge 3$  which is not a double star and  $d_{efev}(G) = q - 2$  for some edge eof G. Then G is unicyclic.

**Proof.** Suppose that *G* is not unicyclic. Then *G* contains more than one cycle. Let  $C_1$  and  $C_2$  be the two cycles of *G*. By Theorem 2.15,  $|C_1| = |C_2| = 3$ .

**Case 1.** Suppose that  $C_1$  and  $C_2$  have exactly one vertex, say, *v* in common.

Let e = uv be an edge of  $C_1$  and let  $S(e) = E(G) - E(C) - \{e, f\}$ , where f = vw, where  $w \in V(C_2)$ . Then S(e) is an edge fixing edge-to-vertex detour set of an edge e of G so that  $d_{efev}(G) = q - 3$ , which is a contradiction.

**Case 2.**Suppose that  $C_1$  and  $C_2$  have a common edge, say, uv. Let e = uv and let  $S(e) = E(G) - \{e, uw, uz\}$ , where  $w \in V(C_1)$  and  $z \in V(C_2)$ . Then S(e) is an edge fixing edge-to-vertex detour set of eofG so that  $d_{efev}(G) = q - 3$ , which is a contradiction.

**Case 3.**Suppose that  $C_1$  and  $C_2$  are connected by a path *P*.

Suppose that e = xu be an edge of  $C_1$ , where x is a vertex common to  $C_1$  are P and let  $S(e) = E(G) - \{e, xu_1, xx_1, f\}$ , where  $xu_1 \in E(C_1)$  such that  $u \neq u_1, xx_1 \in E(P)$  and  $f \in E(C_2)$ . Then clearly S(e) is an edge fixing edge-to-vertex detour set of e of G so that  $d_{efev}(G) \leq q - 4$ , which is a contradiction.

#### Theorem 2.17

For a connected graph G,  $d_{ev}(G) \le d_{efev}(G) + 1$ .

**Proof.** Let *e* be an edge of *G* and S(e) be the minimum edge fixing edge-to-vertex detour set of *e* of *G*. Then  $S(e) \cup \{e\}$  is an edge-to-vertex detour set of *e* of *G* so that  $d_{ev}(G) \leq |S(e) \cup \{e\}| = d_{efev}(G) + 1$ .

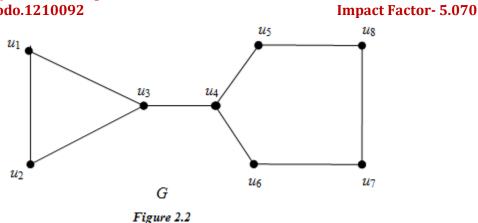
#### Remark 2.18

The bound in Theorem 2.17 is sharp. For the cycle  $C_p$ ,  $d_{efev}(C_p) = 1$  for every  $e \in E(G)$  and  $d_{ev}(G) = 2$  so that  $d_{ev}(G) = d_{efev}(G) + 1$ . Also the inequality in the Theorem 2.17 strict. For the graph G given in Figure 2.2, let  $e = u_3 u_4$ . Then  $S(e) = \{u_1 u_2, u_7, u_8\}$  is an edge fixing edge-to-vertex detour set of e of G so that  $d_{efev}(G) = 2$ . Also  $d_{ev}(G) = 2$ . Hence  $d_{ev}(G) < d_{efev}(G) + 1$ .

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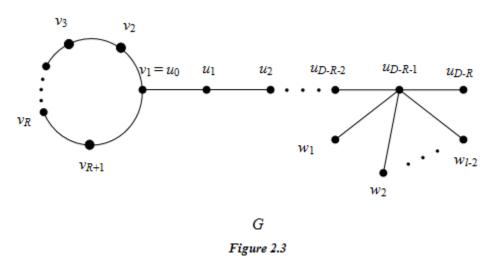


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#### Theorem 2.19

For positive integers R, Dand  $l \ge 2$  with  $R < D \le 2R$ , there exists a connected graph G with rad(G) = R, diam(G) = D and  $d_{efev}(G) = l$  for some  $e \in E(G)$ .

**Proof.** When R = 1, we let  $G = K_{1,l}$ . Then the result follows from Theorem 2.7. Let  $R \ge 2$ . Let  $C_{R+1}: v_1, v_2, ..., v_{R+1}$  be a cycle of length R + 1 and let  $P_{D-R}: u_0, u_1, u_2, ..., u_{D-R}$  be a path of length D - R. Let H be a graph obtained from  $C_{R+1}$  and  $P_{D-R}$  by identifying  $v_1$  in  $C_{R+1}$  and  $u_0$  in  $P_{D-R}$ . Now add l - 2 new vertices  $w_1, w_2, ..., w_{l-2}$  to H and join each  $w_i$   $(1 \le i < l - 2)$  to the vertex  $u_{D-R-1}$  and obtain the graph G as shown in Figure 2.3. Then  $rad_D(G) = R$  and  $diam_D(G) = D$ . Let  $S = \{u_{D-R-1}u_{D-R}, u_{D-R-1}w_1, u_{D-R-1}w_2, ..., u_{D-R-1}w_{l-2}\}$  be the set of end-edges of G. Let e be a non-pendant cut edge of G. By Theorem 2.4, S is a subset of every edge fixing edge-to-vertex detour set of G. It is clear that S is not an edge fixing edge-to-vertex detour set of G and so that  $d_{efev}(G) = l$ .



#### Theorem 2.20

For any positive integer  $a, 1 \le a \le q - 1$ , there exists a connected graph G of size q such that  $d_{efev}(G) = a$ , for some edge  $e \in E(G)$ .

**Proof.** Let *G* be a connected graph.



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**Case 1.**Let a = q - 1. For the star  $G = K_{1,q}$ , by Theorem 6.7, $d_{efev}(G) = q - 1 = a$  for every edge  $e \in E(G)$ .

Case 2.*a* = 1 Let *G* be a path of length *q* and *e* be an pendant-edge of *G*. Then by Theorem 2.7,  $d_{efev}(G) = 1 = a$ .

**Case 3.1** < a < q - 1Let *G* be a tree with *a* end-edges and *q* - *a* internal edges and let *e* be an internal edge of *G*. Then by Theorem 2.7,  $d_{efev}(G) = a$ .

In view of Theorem 2.17, we have the following realization result.

#### Theorem 2.21

For every pair of positive integers with  $2 \le a \le b$ , there exists a connected graph G such that  $d_{ev}(G) = a$  and  $d_{efev}(G) = b$  for some edge  $e \in E(G)$ .

**Proof.** Let *G* be a connected graph.

Case 1.a = b

Let G be a double star with a end-edges and let e be the cut-edge of G. Then by Theorem 2.8,  $d_{efev}(G) = a$ . Also by Theorem 1.2,  $d_{ev}(G) = a$ .

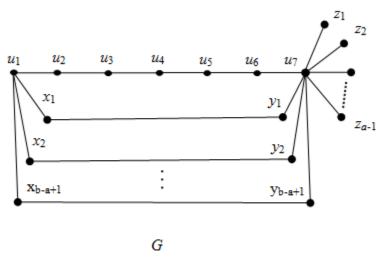
#### Case 2.2 $\leq a < b$

Let  $P: u_1, u_2, u_3, u_4, u_5, u_6, u_7$ , be a path of order 7. Let  $P_i: x_i y_i (1 \le i \le b - a + 1)$  be a copy of a path of order 2. Let H be a graph obtained from the path on P and  $P_i$  by joining  $u_1$  with each  $x_i (1 \le i \le b - a + 1)$  and  $u_7$  with  $y_i (1 \le i \le b - a + 1)$ . Let G be the graph obtained from H by adding new vertices  $z_1, z_2, ..., z_{a-1}$  and joining each  $z_i (1 \le i \le a - 1)$  with  $u_7$ . The graph G is shown in Figure 2.4. First show that  $d_{ev}(G) = a$ . Let S = $\{z_1u_7, z_2u_7, ..., z_{a-1}u_7\}$  be the set of all pendant-edges of G. By Theorem 1.1, S is a subset of every edge-t0vertexdetour set of  $e \circ f G$ . It is clear that S is not an edge-to-vertex detour set of G and so  $d_{ev}(G) \ge a - 1$ . However  $S' = S \cup \{u_6u_7\}$  is an edge-to-vertex detour set of G. Thus  $d_{ev}(G) = a$ . Let  $e = u_1x_1$ . By Theorem2.4,  $S = \{z_1u_7, z_2u_7, ..., z_{a-1}u_7\}$  is a subset of every edge fixing edge-to-vertex detour set of e of G. It is clear that S is not an edge fixing edge-to-vertex detour set of  $e \circ f G$ . It is clear that S is not an edge fixing edge-to-vertex detour set of  $e \circ f G$ . It is clear that S is verticed for <math>G contains  $x_iy_i (2 \le i \le b - a + 1)$  and so  $d_{efev}(G) \ge a - 1 + b - a + 1 = b$ . Let S(e) = $S \cup \{x_1y_1, x_2y_2, ..., x_{b-a+1}, y_{b-a+1}\}$ . Then S(e) is an edge fixing edge-to-vertex detour set of e of G so that  $d_{efev}(G) = b$ . Hence the proof.





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